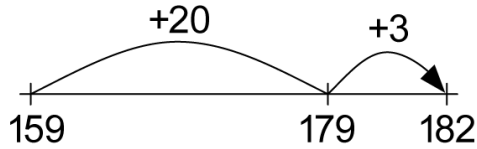


Addition

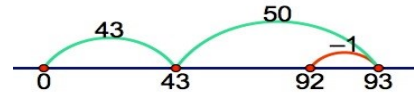
Year 3

Number line, bridging through tens, then hundreds.



Compensating on a number line

$$43 + 49 = ?$$



Expanded partitioning method

$$43 + 24$$

$$40 + 20 = 60$$

$$3 + 4 = 7$$

$$43 + 24 = 67$$

Column addition up to 3 digits

$$\begin{array}{r} 367 \\ + 85 \\ \hline 452 \\ 11 \end{array}$$

Year 4

Column addition up to 4 digits

$$\begin{array}{r} 4324 \\ + 4256 \\ \hline 8580 \\ 1 \end{array}$$

Year 5

Column addition (decimals)

H	T	O	1/10	1/100
		4	2	3
		3	1	4
		7	3	7

Year 6

Column addition up to any digits

$$\begin{array}{r} 432438 \\ + 25653 \\ \hline 458091 \\ 11 \end{array}$$

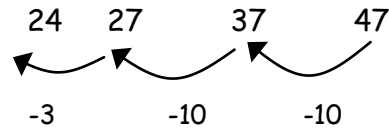
Add decimals with different decimal places (e.g. $4.384 + 2.66$)

$$\begin{array}{r} 4.384 \\ + 2.660 \\ \hline 7.044 \\ 11 \end{array}$$

Subtraction

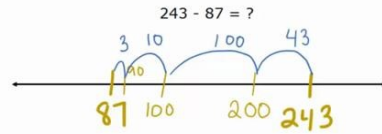
Year 3

Counting back on a number line



Counting on method

Subtraction is finding the **difference**, or **distance** between two numbers.



Partitioning and decomposition

$$\begin{array}{r}
 89 - 57 \\
 89 = 80 + 9 \\
 - 57 \quad 50 + 7 \\
 \hline
 30 + 2 = 32
 \end{array}$$

Formal column method

$$\begin{array}{r}
 6141 \\
 - 754 \\
 \hline
 668
 \end{array}$$

Year 4

Formal column method up to 4 digits

$$\begin{array}{r}
 6141 \\
 - 754 \\
 \hline
 6683
 \end{array}$$

Year 5

Formal column method with 4 digits or more

$$\begin{array}{r}
 6141 \\
 - 754 \\
 \hline
 6683
 \end{array}$$

Year 6

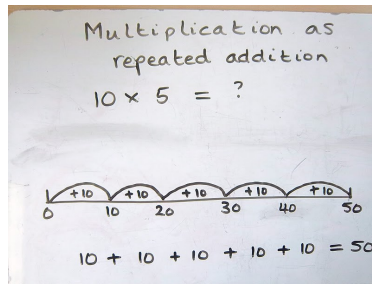
Formal column method - decomposition (including decimals)

$$\begin{array}{r}
 1101 \\
 21.18 \\
 - 8.43 \\
 \hline
 12.75
 \end{array}$$

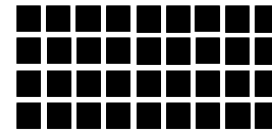
Multiplication

Year 3

Repeated addition



Arrays



$$4 \times 9 = 36$$

$$9 \times 4 = 36$$

Grid Method TO x Ones 23×8

$$\begin{array}{r} \times \quad 20 \quad 3 \quad 160 \\ 8 \quad \boxed{160} \quad \boxed{24} \quad + \quad \underline{24} \\ \hline 184 \end{array}$$

Progress to Short multiplication

$$\begin{array}{r} \quad 2 \quad 4 \\ \times \quad \quad 6 \\ \hline 1 \quad 4 \quad 4 \\ \hline \quad 2 \end{array} \quad \begin{array}{r} \quad 3 \quad 4 \quad 2 \\ \times \quad \quad \quad 7 \\ \hline 2 \quad 3 \quad 9 \quad 4 \\ \hline \quad 2 \quad 1 \end{array}$$

Year 4

Grid Method HTO x O, TO x TO

x	70	2
30	2100	60
8	560	16

Short multiplication to 4 digits

$$\begin{array}{r} \quad 2 \quad 4 \\ \times \quad \quad 6 \\ \hline 1 \quad 4 \quad 4 \\ \hline \quad 2 \end{array} \quad \begin{array}{r} \quad 3 \quad 4 \quad 2 \\ \times \quad \quad \quad 7 \\ \hline 2 \quad 3 \quad 9 \quad 4 \\ \hline \quad 2 \quad 1 \end{array}$$

Year 5

Grid method ThHTO x O

$$\begin{array}{r} \times \quad 1000 \quad 300 \quad 40 \quad 6 \quad 9000 \\ 9 \quad \boxed{9000} \quad \boxed{2700} \quad \boxed{360} \quad \boxed{54} \quad + \quad 360 \\ \hline \quad \quad \quad \quad \quad + \quad 54 \\ \hline \quad \quad \quad \quad \quad \underline{12114} \\ \quad \quad \quad \quad \quad \quad 1 \quad 1 \end{array}$$

Grid method O th x O

$$\begin{array}{r} \times \quad \quad 4 \quad 0.9 \quad 12 \\ 3 \quad \boxed{12} \quad \boxed{2.7} \quad + \quad \underline{2.7} \\ \hline \quad \quad \quad \quad \quad \underline{14.7} \end{array}$$

Long multiplication of 2 digit numbers TO X TO

$$\begin{array}{r} \quad 24 \\ \times 16 \\ \hline \quad 24 \quad (6 \times 4) \\ 120 \quad (6 \times 20) \\ \hline 200 \quad (10 \times 4) \\ 240 \quad (10 \times 20) \\ \hline 384 \end{array} \quad \begin{array}{r} \quad 24 \\ \times 16 \\ \hline \quad 144 \quad (6 \times 24) \\ 240 \quad (10 \times 24) \\ \hline 384 \end{array}$$

Year 6

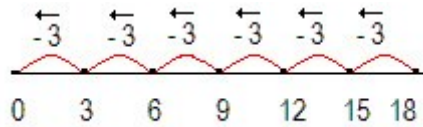
Long multiplication to 4 digit numbers

$$\begin{array}{r} \quad 1 \quad 2 \quad 4 \\ \times \quad 5 \quad 6 \\ \hline \quad 7 \quad 4 \quad 4 \\ \quad 1 \quad 2 \\ \hline \quad 7 \quad 4 \quad 4 \quad 0 \\ \quad 1 \quad 2 \\ \hline \quad 8 \quad 1 \quad 8 \quad 4 \\ \quad 1 \end{array}$$

Division

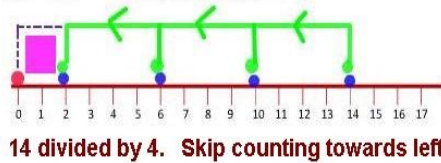
Year 3

Repeated subtraction using a number line



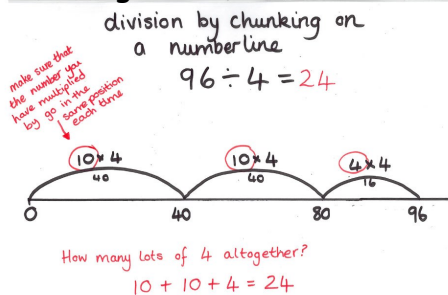
....with remainders

Remainder = 2 Quotient = 3



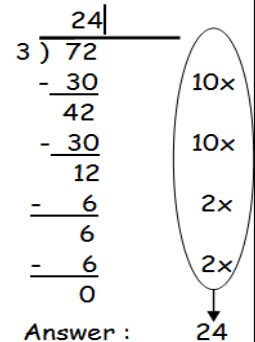
Year 4

Chunking on a number line



Vertical chunking method

$$72 \div 3$$



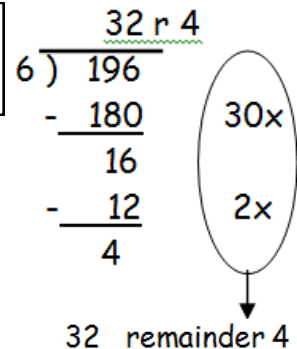
Formal short division

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \end{array}$$

Year 5

Chunking with remainders

$$196 \div 6$$



Year 5

Formal short division including remainders

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \end{array}$$

Year 6

Long Division

