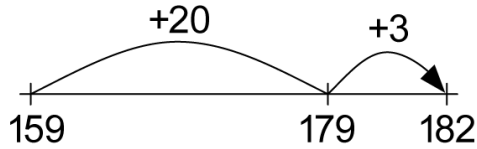


Addition

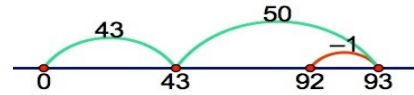
Year 3

Number line, bridging through tens, then hundreds.



Compensating on a number line

$$43 + 49 = ?$$



Expanded partitioning method

$$\begin{array}{r} 43 + 24 \\ 40 + 20 = 60 \\ 3 + 4 = 7 \\ \hline 43 + 24 = 67 \end{array}$$

Column addition up to 3 digits

$$\begin{array}{r} 367 \\ + 85 \\ \hline 452 \\ 11 \end{array}$$

Year 4

Column addition up to 4 digits

$$\begin{array}{r} 4324 \\ +4256 \\ \hline 8580 \\ 1 \end{array}$$

Year 5

Column addition (decimals)

H	T	O	1/10	1/100
		4	2	3
		3	1	4
		7	3	7

Year 6

Column addition up to any digits

$$\begin{array}{r} 432438 \\ + 25653 \\ \hline 458091 \\ 11 \end{array}$$

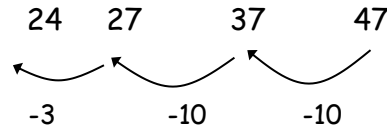
Add decimals with different decimal places (e.g. $4.384 + 2.66$)

$$\begin{array}{r} 4.384 \\ +2.660 \\ \hline 7.044 \\ 11 \end{array}$$

Subtraction

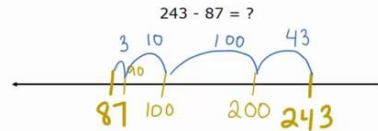
Year 3

Counting back on a number line



Counting on method

Subtraction is finding the **difference**, or **distance** between two numbers.



Partitioning and decomposition

$$\begin{array}{r} 89 - 57 \\ 89 = 80 + 9 \\ - 57 \quad 50 + 7 \\ \hline 30 + 2 = 32 \end{array}$$

Formal column method

$$\begin{array}{r} 6 \ 14 \ 1 \\ 7 \ 5 \ 4 \\ - \quad 8 \ 6 \\ \hline 6 \ 6 \ 8 \end{array}$$

Year 4

Formal column method up to 4 digits

$$\begin{array}{r} 6141 \\ 7645 \\ - \quad 862 \\ \hline 6683 \end{array}$$

Year 5

Formal column method with 4 digits or more

$$\begin{array}{r} 6141 \\ 7645 \\ - \quad 862 \\ \hline 6683 \end{array}$$

Year 6

Formal column method - decomposition (including decimals)

$$\begin{array}{r} 1 \ 10 \ 1 \\ 2 \ 1.1 \ 8 \\ - \quad 8.4 \ 3 \\ \hline 1 \ 2.7 \ 5 \end{array}$$

Subtract decimals with different decimal places

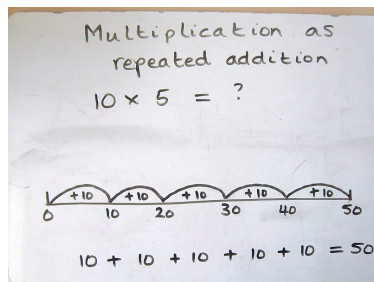
(e.g. $4.984 - 2.66$)

$$\begin{array}{r} 4.984 \\ - 2.660 \\ \hline 2.324 \end{array}$$

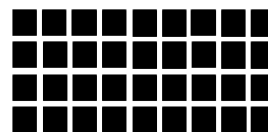
Multiplication

Year 3

Repeated addition



Arrays



$$4 \times 9 = 36$$

$$9 \times 4 = 36$$

Grid Method TO x Ones 23×8

$$\begin{array}{r} \times \quad 20 \quad 3 \quad 160 \\ 8 \quad \boxed{160} \quad \boxed{24} \quad + \quad \underline{24} \\ \hline 184 \end{array}$$

Progress to Short multiplication

$$\begin{array}{r} 23 \\ \times 8 \\ \hline 24 \quad (8 \times 3) \\ 160 \quad (8 \times 20) \\ \hline 184 \end{array} \quad \begin{array}{r} 3 \quad 4 \quad 2 \\ \times \quad \quad 7 \\ \hline 2 \quad 3 \quad 9 \quad 4 \\ \hline 2 \quad 1 \end{array}$$

Year 4

Grid Method HTO x O , TO x TO

x	70	2
30	2100	60
8	560	16

Short multiplication to 4 digits
Expanded method

$$\begin{array}{r} 123 \\ \times 8 \\ \hline 24 \quad (8 \times 3) \\ 160 \quad (8 \times 20) \\ 200 \quad (8 \times 100) \\ \hline 384 \end{array} \quad \begin{array}{r} 3 \quad 4 \quad 2 \\ \times \quad \quad 7 \\ \hline 2 \quad 3 \quad 9 \quad 4 \\ \hline 2 \quad 1 \end{array}$$

Year 5

Grid method ThHTO x O

$$\begin{array}{r} \times \quad 1000 \quad 300 \quad 40 \quad 6 \quad 9000 \\ 9 \quad \boxed{9000} \quad \boxed{2700} \quad \boxed{360} \quad \boxed{54} \quad + \quad 360 \\ \hline 12114 \end{array}$$

Short multiplication to 5 digits
(see Y4)

Grid method O th x O

$$\begin{array}{r} \times \quad 4 \quad 0.9 \quad 12 \\ 3 \quad \boxed{12} \quad \boxed{2.7} \quad + \quad 2.7 \\ \hline 14.7 \end{array}$$

Long multiplication of 2 digit numbers TO X TO

$$\begin{array}{r} 24 \\ \times 16 \\ \hline 24 \quad (6 \times 4) \\ 120 \quad (6 \times 20) \\ 40 \quad (10 \times 4) \\ 200 \quad (10 \times 20) \\ \hline 384 \end{array} \quad \begin{array}{r} 24 \\ \times 16 \\ \hline 144 \quad (6 \times 24) \\ 240 \quad (10 \times 24) \\ \hline 384 \end{array}$$

Year 6

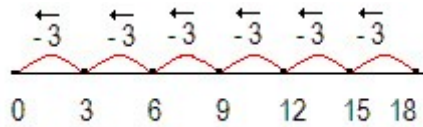
$$\begin{array}{r} 124 \\ \times 56 \\ \hline 744 \\ 6200 \\ \hline 6968 \end{array}$$

Long multiplication to 4 digit numbers

Division

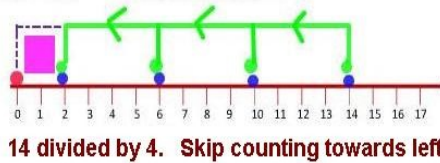
Year 3

Repeated subtraction using a number line



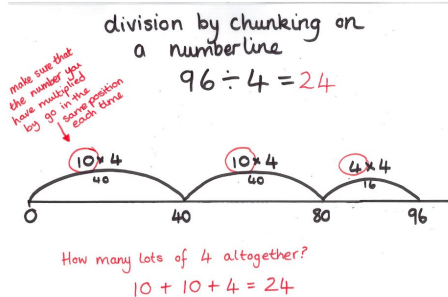
....with remainders

Remainder = 2 Quotient = 3



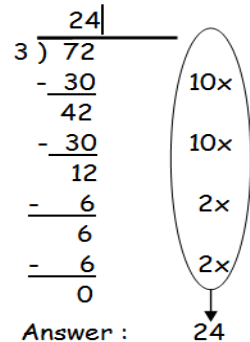
Year 4

Chunking on a number line



Vertical chunking method

$$72 \div 3$$



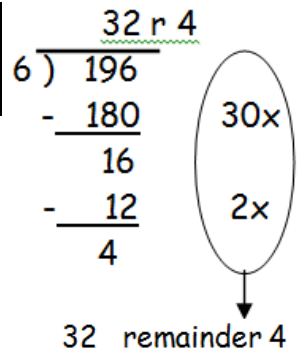
Formal short division

$$\begin{array}{r} 14 \\ 7 \overline{) 98} \\ \underline{7} \\ 28 \\ \underline{28} \\ 0 \end{array}$$

Year 5

Chunking with remainders

$$196 \div 6$$



Year 5

Formal short division including remainders

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \\ \underline{40} \\ 32 \\ \underline{30} \\ 2 \end{array}$$

Year 6

Long Division

